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# TWO-DIMENSIONAL IMAGING VELOCITY INTERFEROMETRY: TECHNIQUE AND DATA ANALYSIS 

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#### Abstract

We describe the data analysis procedures for an emerging interferometric technique for measuring motion across a two-dimensional image at a moment in time, i.e. a snapshot 2d-VISAR.


Keywords: VISAR, velocity interferometry
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## INTRODUCTION

Velocity interferometers (VISAR) measuring target motion to high precision have been an important diagnostic in shockwave physics for many years[1, 2, 3, 4]. Until recently, this diagnostic has been limited to measuring motion at points or lines across a target. We introduce an emerging interferometric technique for measuring motion across a two-dimensional image, which could be called a snapshot 2d-VISAR.
If a sufficiently fast movie camera technology existed, it could be placed behind a traditional VISAR optical system and record a 2 d image vs time. But since that technology is not yet available, we use a CCD detector to record a single 2 d image, with the pulsed nature of the illumination providing the time resolution.

Consequently, since we are using pulsed illumination having a coherence length shorter than the VISAR interferometer delay ( $\sim 0.1 \mathrm{~ns}$ ), we must use the white light velocimetry configuration to produce fringes with significant visibility[5, 6, 7]. In this scheme, two interferometers (illuminating, detecting) having nearly identical delays are used in series, with one before the target and one after. This produces fringes with at most $50 \%$ visibility, but otherwise has the same fringe shift per target motion of a traditional VISAR.


FIGURE 1. Trigonal symmetry of a spherical wave emerging from 1 mm thick Si along the [111] direction is immediately apparent with an 2d-imaging VISAR. The 2dVISAR allows a whole new world of data not accessible by point or line-VISARs. Field of view $\sim 1 \mathrm{~mm}$.

The 2d-VISAR observes a new world of information (Fig. 1) about shock behavior not readily accessible by traditional point or 1d-VISARS, simultaneously providing both a velocity map and an "ordinary" snapshot photograph of the target. The 2d-VISAR has been used to observe nonuniformities in NIF related targets (polycrystalline diamond, Be ) [8, 9], and in Si (Fig. 1) and Al (Fig. 4).

## DATA PROCESSING STEPS

1. Split into quads. The original $4096 x 4096$ sized image from the CCD detector is split into four quadrants of $2000 \times 2000$ size, rotating to overlay.
2. Overlay quads. Sections of each quadrant are correlated to find rotation, translation, magnification. The result is a stack of images having four intensities $S_{n}$ per pixel. The correlation peak width can be $\sim 3$ pixels, indicating focus quality. Correlations usually can be done on shot exposure.
3. Lissajous analysis. A 1d-lineout is taken, usually in the undriven area where the fringe phase is well behaved, perpendicular to the bias fringes, and $>1$ period ( $\sim 100$ pixels). A Lissajous plot of $F$ (Fig. 6, top) is made of the combined four channels (via Eqs. 2-10) and the gains and offsets adjusted until the Lissajous is centered and circular. Under changing $I$ it helps to plot $|F|$ vs $I$ plot (Fig. 6, bottom) for best linearity.
3b. (Optional) Spatial dependence. Repeat above step at different locations to find any spatial dependence to optimal gains. Often the spatial dependence is weak and we approximate gains as constants for expediency. Appearance of the bias fringe periodicity or 2 nd harmonic in any 2 d-outputs (below) indicates gains not optimal.
4. Math applied to $2 d$ data. The optimal gains are applied to the 2d data via Eqs. 2-12 to produce intensity $I(x, y)$, the complex fringing field $F(x, y)$, wrapped phase $\theta(x, y)$, and magnitude $|F(x, y)|$.
$4 b$. (Optional) Removal of bias phase slope. The constant slope in phase due to due tilted interferometer mirror causes the FFT of $F$ to translate. Thus one can easily remove the bias slope by identifying what would be the DC spike, translating the FFT so that this spike is at the origin. However, the bias slope is useful to keep for Lissajous display purposes, and for manifesting contours in the wrapped phase map (Fig. 4), so we often postpone removing it.
5. (Optional) Fourier power spectra The Fourier spectrum of $F(x, y) /|F(x, y)|$ can be immediately taken (not needing the problematic unwrapping step below), to characterize the phase (velocity) roughness. An FFT of $I(x, y)$ characterizes the ordinary image. The FFT can be taken on subsets of the image to provide some spatial dependence.
6. Unwrapping of phase map. Where integer fringe skips are encountered they are restored to produce a continuous surface of phase. However, noise


FIGURE 2. Raw image from CCD detector records four interferometer outputs ideally having $90^{\circ}$ phase interval between them.
in low intensity areas (due to laser speckle) produces areas of wildly fluctuating phase which confuses most algorithms. (Hence the granular appearance of Fig. 7.) This problem is still being explored.

## Supporting equations

The interferometer output for the channels $n$ is

$$
\begin{equation*}
S_{n}(x, y)=I(x, y)\left\{1+0.5 \gamma \cos 2 \pi\left[\theta(x, y)+\phi_{n}\right]\right\} \tag{1}
\end{equation*}
$$

The four output channel phases $\phi_{n}$ are ideally in $90^{\circ}$ intervals, but often irregular by $\sim 30^{\circ}$. Irregularity is handled by the obliquity correction Eq. 9. The visibility $\gamma$ decreases from 1 by interferometer misalignment, or target surface quality under shock loading. The 0.5 maximum fringe contrast is appropriate for the partial coherence of white light velocimetry. The target reflected intensity is $I(x, y)$, and detected intensity post-interferometer $S(x, y)$. Channel dependent transmission loss through the optics is represented by gain coefficients in Eqs. 2-4 etc.

The equations below for combining the four detected signals $S_{n}$ into fringing $F$ and nonfringing $I$ outputs are the same for each pixel, and thus we can omit the $(x, y)$. As a first approximation the gains $g_{n}$
and offsets $h_{0}, v_{0}$ are constants, but should eventually model any slight spatial variation of beam intensities.

$$
\begin{align*}
S_{0}^{\prime} & =\left(g_{02} S_{0}+h_{0}\right) g_{h v}  \tag{2}\\
S_{1}^{\prime} & =\left(g_{13} S_{1}+v_{0}\right)  \tag{3}\\
S_{2}^{\prime} & =g_{h v} S_{2}  \tag{4}\\
S_{3}^{\prime} & =S_{3} \tag{5}
\end{align*}
$$

The two intermediate outputs are the nonfringing intensity $I$ and the complex fringing field $F$

$$
\begin{align*}
& I=0.25\left(S_{0}^{\prime}+S_{1}^{\prime}+S_{2}^{\prime}+S_{3}^{\prime}\right)  \tag{6}\\
& F=\left(S_{0}^{\prime}-S_{2}^{\prime}\right)+i\left(S_{1}^{\prime}-S_{3}^{\prime}\right) \tag{7}
\end{align*}
$$

It is useful to confirm that $I_{v}=S_{0}^{\prime}+S_{2}^{\prime}$ appears like $I_{h}=S_{1}^{\prime}+S_{3}^{\prime}$. Otherwise you have a bad channel.
The obliquity transform fixes irregular phase steps. Temporarily change coordinates to a $45^{\circ}$ axis, and apply an astigmatic correction $g_{q}$ along the new axis. Typically $g_{q} \sim 0.6$ to 1 .

$$
\begin{align*}
\mathfrak{R} F & \leftarrow 0.5\left\{\left(g_{q}+1\right) \mathfrak{\Re} F+\left(g_{q}-1\right) \mathfrak{I} F\right\}  \tag{8}\\
\mathfrak{R} I & \leftarrow 0.5\left\{\left(g_{q}-1\right) \mathfrak{R} F+\left(g_{q}+1\right) \mathfrak{I} F\right\}  \tag{9}\\
F & \leftarrow \mathfrak{R} F+i \mathfrak{I} F \tag{10}
\end{align*}
$$

The offsets $h_{0}, v_{0}$, translate the Lissajous ( $\mathfrak{J} F$ vs $\mathfrak{R} F$ ). The horizontal to vertical astigmatism $g_{h v}$ stretches the Lissajous. The left/right asymmetry $g_{02}$ and up/down asymmetry $g_{13}$ are degenerate with offsets $h_{0}, v_{0}$ when Lissajous magnitude $(|F|)$ is constant, and are only relevant when the magnitude changes significantly. In that case, one first adjusts the offsets to center the weakest intensity portions of the Lissajous, and then uses $g_{02}$ and $g_{13}$ to center the outer portions.
The gains and offsets are adjusted until the Lissajous is centered and circular. To make this determination independent of fluctuating $I$, one plots $|F|$ vs $I$ and minimizes deviations from linearity.

After one is satisfied with choice of gains and offset (by obtaining a circular and centered Lissajous), then the magnitude $|F|$ and phase $\theta$ is

$$
\begin{gather*}
|F|^{2}=(\mathfrak{I F})^{2}+(\Re F)^{2}  \tag{11}\\
2 \pi \tan \theta=\frac{\mathfrak{J} F}{\mathfrak{\Re} F} \tag{12}
\end{gather*}
$$

obtained for every pixel. This will be proportional to the target velocity as in a traditional VISAR (in the short etalon approximation).


FIGURE 3. The snapshot "ordinary" image of target, $I(x, y)$, simultaneous with phase measurement (Fig. 4), formed by summing the four quadrature images so that fringes cancels. Field of view is $\sim 1 \mathrm{~mm}$ per 2000 pixels. Target is $50 \mu \mathrm{~m}$ of aluminum facing vacuum. The fine striations are machining scratches. The corner of the square target is centered on the image.


FIGURE 4. Snapshot phase (velocity) map of target simultaneous to ordinary image (Fig. 3). The interesting velocity variations in the target may be due to aluminum granular domains. The undriven side of the image has the uniform bias fringes. Phase is wrapped.


FIGURE 5. Wrapped phase map subset.


FIGURE 6. Optimal gain parameters (red curves) produce the most circular Lissajous, $\mathfrak{J} F$ vs $\mathfrak{R} F$ (top), and most linear $|F|$ vs intensity $I$ (bottom).

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FIGURE 7. Phase map after some fringe skips removed by a commercial algorithm (Wavemetrics, Igor application). Algorithm is confused by many regions of low intensity where noise causes wild variation in phase.

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